

INTERNATIONAL INDIAN SCHOOL BURAI DAH
MATHS-XII/WS Continuity and Differentiability-2025-26

1-If the function f defined as $f(x) = \begin{cases} \frac{x^2-9}{x-3}, & x \neq 3 \\ k, & x = 3 \end{cases}$ is continuous at $x=3$, find the value of k .
Ans : $k=6$ (CBSE-2020)

2- Find the value of k if the function $f(x) = \begin{cases} \frac{\sin 5x}{3x} + \cos x, & x \neq 0 \\ k, & x = 0 \end{cases}$ is continuous at $x=0$
Ans : $k= 8/3$ (CBSE-2017)

3-Find the value of k if the function $f(x) = \begin{cases} \frac{kx}{|x|}, & x < 0 \\ k, & x \geq 0 \end{cases}$ is continuous at $x=0$
Ans : $k= -3$ (CBSE-2017)

4- Find the value of λ if the function $f(x) = \begin{cases} \frac{\sin^2 \lambda x}{x^2}, & x \neq 0 \\ 1, & x = 0 \end{cases}$ is continuous at $x=0$
Ans : $\lambda = \pm 1$ (CBSE-2023)

5- If $f(x) = \begin{cases} x^2, & \text{if } x \geq 1 \\ x, & \text{if } x < 1 \end{cases}$ then show that f is not differentiable at $x=1$ (CBSE-2023)

6- Differentiate $\sin^2(\sqrt{x})$ with respect to x (CBSE-2020)

7- If $y = 2\sqrt{\sec(e^{2x})}$ then find $\frac{dy}{dx}$ (CBSE-2020)

8- If $y = \operatorname{Cosec}(\cot \sqrt{x})$ then find $\frac{dy}{dx}$ (CBSE-2020)

9- If $y = 5e^{7x} + 6e^{-7x}$, show that $\frac{d^2y}{dx^2} = 49y$ (CBSE-2019)

10- If $y = (x + \sqrt{x^2 - 1})^2$, then show that $(x^2 - 1)\left(\frac{dy}{dx}\right)^2 = 4y^2$ (CBSE-2023)

11- If $(x^2 + y^2)^2 = xy$ then find $\frac{dy}{dx}$ (CBSE-2023)

12- If $y = x^{\frac{1}{x}}$, then find $\frac{dy}{dx}$ at $x=1$ (CBSE-2023)

13- If $x = a \sin 2t, y = a(\cos 2t + \log \tan t)$, then find $\frac{dy}{dx}$ (CBSE-2023)

14- If $x = at^2$, $y = 2at$, then find $\frac{d^2y}{dx^2}$ (CBSE-2020)

15- If $f(x) = \sqrt{\tan\sqrt{x}}$, then find $f'(\frac{\pi^2}{16})$ (CBSE-2020)

16- If $y = \sqrt{ax + b}$, prove that $y(\frac{d^2y}{dx^2}) + (\frac{dy}{dx})^2 = 0$ (CBSE-2023)

17- Differentiate $\tan^{-1}\frac{3x - x^3}{1 - 3x^2}$ w.r.t $\tan^{-1}\frac{x}{\sqrt{1-x^2}}$ (CBSE-2019)

18- If $(\cos x)^y = (\cos y)^x$ then find $\frac{dy}{dx}$ (CBSE-2012,2024)

19- If $\sqrt{1-x^2} + \sqrt{1-y^2} = a(x-y)$ then show that $\frac{dy}{dx} = \sqrt{\frac{1-y^2}{1-x^2}}$
(CBSE-2009,19,24)

20- If $y = (\tan^{-1} x)^2$, show that $(x^2 + 1)^2 y_2 + 2x(x^2 + 1)y_1 = 2$ (CBSE-2012)

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